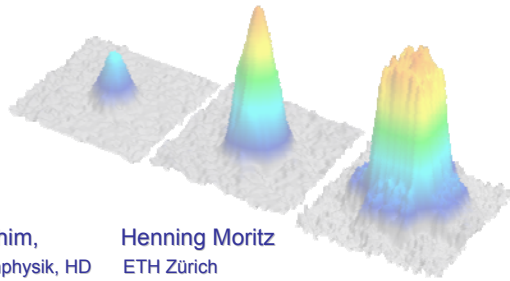


**Creating new states of matter:
Experiments with ultra-cold Fermi gases**



Selim Jochim,
MPI für Kernphysik, HD

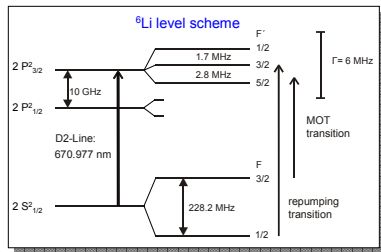
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Outline

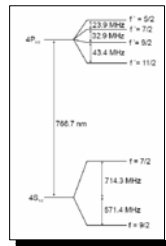
- Cooling (difficulties) with Fermions
- Scattering
- Concept of Feshbach resonances
- Ultracold molecules
- Making a BEC of molecules

Fermionic Alkalis

Only ${}^6\text{Li}$ and ${}^{40}\text{K}$ stable fermions

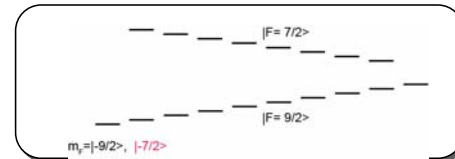
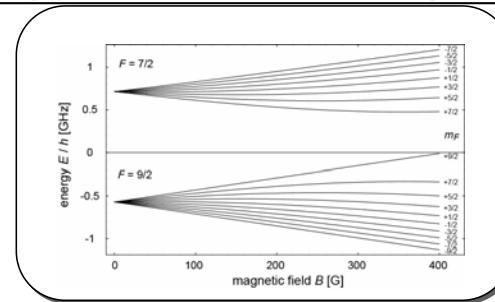


${}^6\text{Li}$, rel. isotope abundance in Li=7%
 $l=1$, melting point $\sim 180^\circ\text{C}$

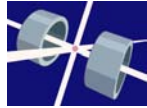


${}^{40}\text{K}$, abundance=0.01%
 $l=4$, melting point $\sim 60^\circ\text{C}$

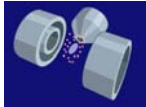
Magnetic field dependence (e.g. ${}^{40}\text{K}$)



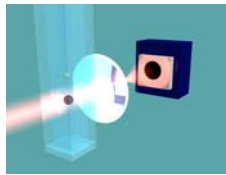
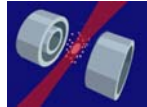
Cooling Methods



Laser cooling
~0.1 mK
~10⁸ atoms



Evaporative cooling
in magnetic trap
or dipole trap
T < 100 nK < T_F, 10⁸ atoms



Absorption
imaging

Ideal Fermi Gas in an harmonic trap

$$f(\varepsilon) = \frac{1}{\exp\left(\frac{\varepsilon - \mu}{kT}\right) - 1}$$

$$D(\varepsilon) = \frac{\varepsilon^2}{2(\hbar\omega)^3} \quad \text{3D harmonic oscillator}$$

$$N = \int_0^\infty D(\varepsilon) f(\varepsilon) d\varepsilon$$

$$\Rightarrow E_F = k_B T_F = \hbar\omega(6N)^{1/3} \sim 0.1 - 1 \mu\text{K}$$

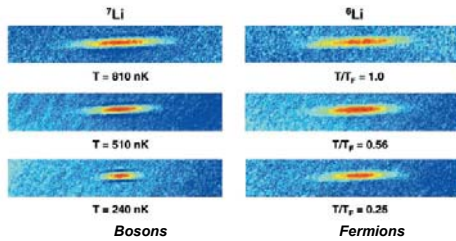
$$k_F = \sqrt{2mE_F} = (6\pi^2 n_0)^{1/3}$$

$$n_0^{-1/3} \approx 0.3 - 1 \mu\text{m}$$

$$R_F = a_{ho}(48N)^{1/6}$$

$$\approx 10 - 100 \mu\text{m}$$

Sympathetic Cooling



BEC has no entropy, only thermal atoms
 \Rightarrow heat capacity vanishes for $T \rightarrow 0$
 $N_{th}, C_{BEC} \sim \left(\frac{T}{T_C}\right)^3$

For Fermions

$$C_{Fermi} \sim \frac{T}{T_F}$$

A. G. Truscott, K. E. Strecker, W. I. McAlexander, G. B. Partridge, R. G. Hulet, Science 291, 2570 (2001);

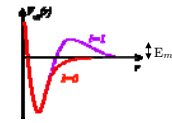
The difficulty in cooling fermions

Collisions are required for cooling, but at low T
 spin polarised fermions stop colliding



Two particle wavefunction: $\Psi_{1,2} = \chi_{\text{spin}} \cdot \psi_{\text{space}}$

Partial wave expansion: $\psi_{\text{space}} = \psi_{\text{s-wave}} + \psi_{\text{p-wave}}$
 symmetric anti-symmetric



Only s-wave collisions energetically possible
 $\Rightarrow \chi_{\text{spin}}$ antisymmetric \Rightarrow spin mixture

$$mv \cdot r_{\text{eff}} = \hbar$$

$$\Rightarrow E_{\text{min}} = 1/2mv^2 = \frac{\hbar^2}{mr_{\text{eff}}^2}$$

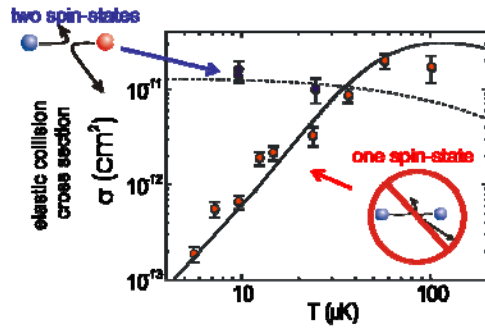
$$\approx 10 - 100 \mu\text{K}$$

$$\psi(r) \sim \frac{e^{ikr} + f(k, \theta)e^{ikr}}{r}$$

$$\sigma = \int_{\Omega} |f(k, \theta)|^2 d\Omega$$

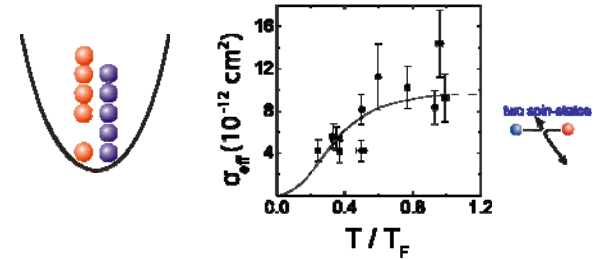
$$\sigma_l \propto k^{2l}; \quad \sigma_s = 4\pi a^2$$

Collision cross-sections



B. DeMarco *et al.*, PRL 82, 4208 (1999)

Pauli Blocking of Collisions



Collisions die out at low T
Cooling difficult! Limit $T \sim 20\% T_F$

B. deMarco, S. Papp, D. S. Jin, PRL 86, 5409 (2001);

Condition for Superfluidity

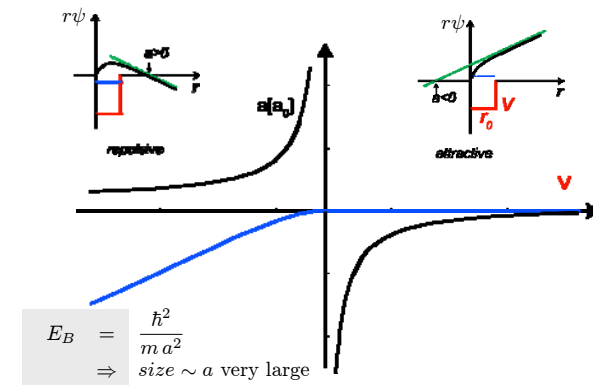
$$T_{BCS} \approx 0.2 T_F \exp\left(-\frac{\pi}{2k_F |a|}\right)$$

- $a < 0 \Rightarrow$ attractive interaction
- $k_F \propto n^{1/3} \sim 1/\text{mean distance}$
- $k \cdot |a| < 1 \Rightarrow T_{BCS} \ll T_F$

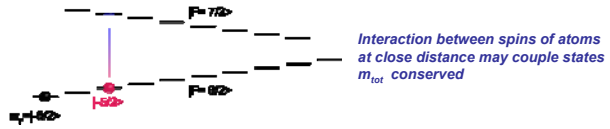
Still a long way to go:

Interaction strength $\sim a$ an important parameter:
 • increases T_C
 • makes cooling more efficient

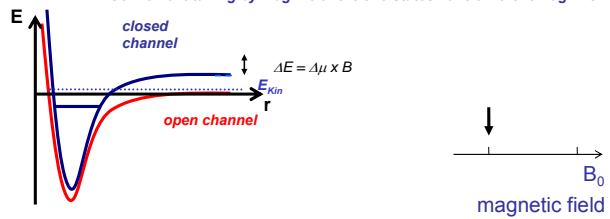
Scattering length and bound states



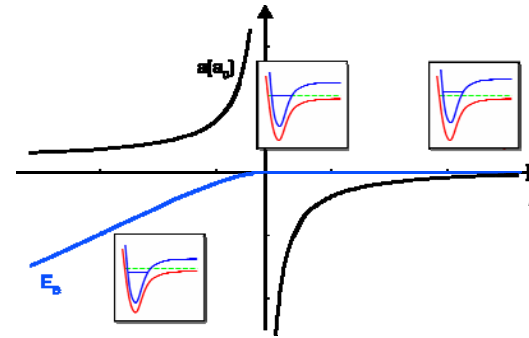
Feshbach resonance



- Tune bound state of a "closed channel" into degeneracy with the continuum
- Convenient tuning by mag. field: the two states have different mag. moment



Scattering length and bound states



Composite Bosons

Free Fermions

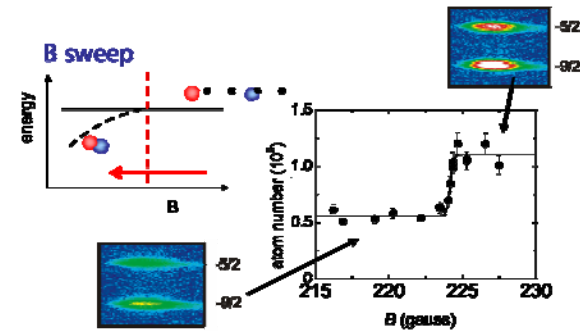
How to see the molecules?

Molecules have different optical transition frequency

Why: If one constituent is excited, its dipole couples resonantly polarises the other \Rightarrow Potential between two dipoles $\sim R^{-3}$, R molecule size

$$\text{Shift} \approx \hbar\Gamma \left(\frac{\lambda}{2\pi R}\right)^3$$

How to see the molecules?



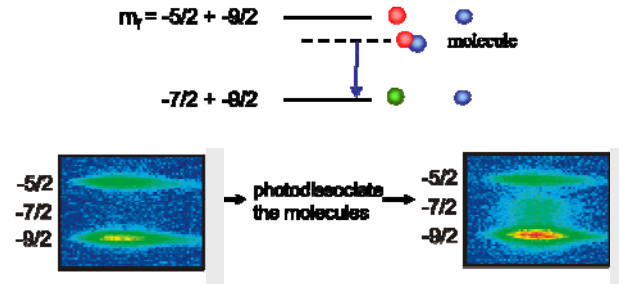
C. A. Regal et al., Nature 424, 47 (2003).

Motivation: E. A. Donley et al., Nature 417, 529 (2002)

RF Photodissociation

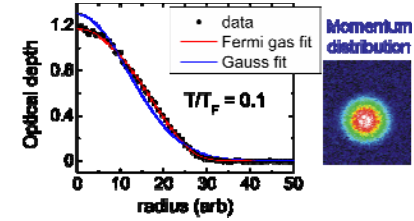
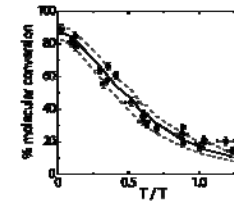
rf photodissociation

Apply rf near the atomic $m_f = -5/2$ to $m_f = -7/2$ transition



C. A. Regal et al., Nature 424, 47 (2003).

Molecule Fraction and Temperature



$$OD(x, y) = OD_0 \cdot Li_2(-\zeta e^{-\frac{x^2}{2a^2} - \frac{y^2}{2a^2}}) / Li_2(-\zeta)$$

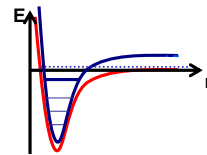
$$\zeta = \exp(-T/T_F) \quad Li_n(x) = \sum_{k=1}^{\infty} x^k / k^n$$

E. Hodby et al. PRL 94, 120402 (2005);

From Jin Group, JILA, Boulder

Stability of molecules

Fermionic molecules are surprisingly stable
Bosonic not



Pauli Blocking prevents the atoms from coming close



Decay rate $\sim \left(\frac{\text{Size of Potential}}{\text{Molecule size}} \right)^3 \sim a^{-3}$

Short summary

• The bad news:

- Sympathetic cooling difficult, because heat capacity of BEC vanishes
- Direct cooling of Fermions: Only s-wave collisions at low T
- become Pauli blocked at low T

End of 2001

• The good news

- T_c and rethermalisation depends on a tunable via Feshbach resonance
- Two fermions transform into one composite Boson across resonance
- molecules long lived

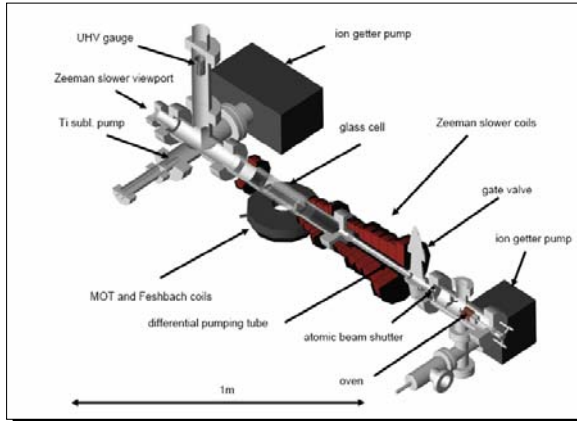
Spring of 2003

Two Solutions

Cool very hard with Fermions

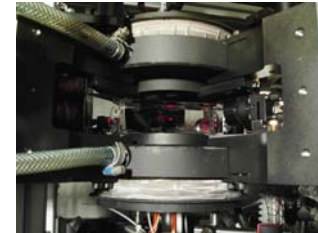
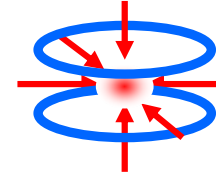
Cooling on the Bosonic side

A machine to produce cold Fermions



Experimental procedure

- Magneto-optical Trap



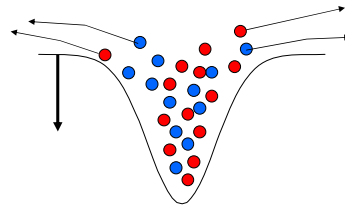
Optical dipole traps

Dipole potential:

$$U_{dip} = -\frac{1}{2} \langle p \cdot E \rangle$$



focused beam trap



cooling performed by evaporation:
simply lower the trap power!

Different sizes

⁶Li MOT

100 million atoms
200 μ K
Radius \sim 1mm



"funnel" needed
for efficient loading

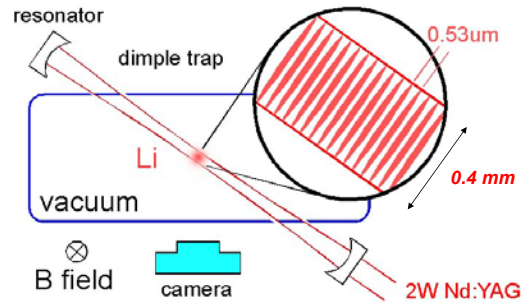
near-infrared laser
=1.03 μ m, max. 10W

beam waist 25 μ m
trap depth \sim 1mK

Funnel

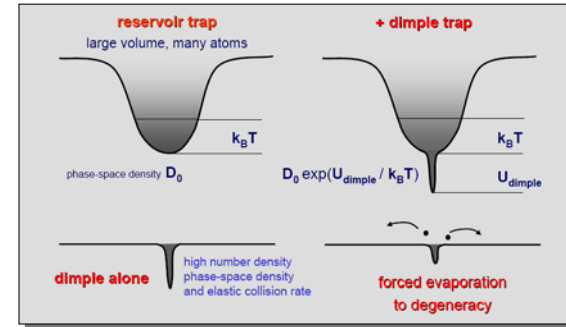
Use resonant enhancement in an optical resonator:

- ~130-fold enhancement
- Deep and large volume trap

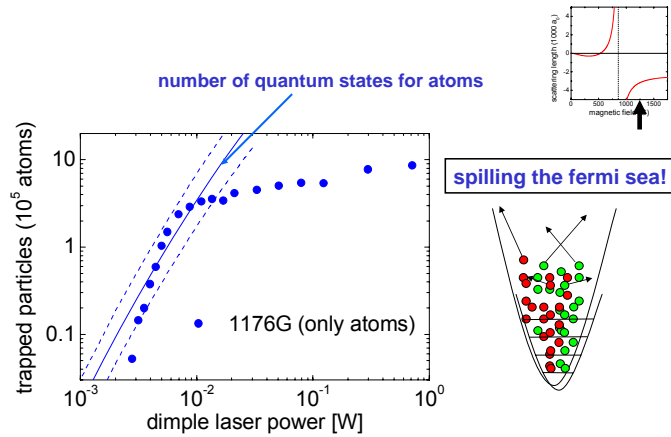


Mosk *et al.*, Opt. Lett 26, 1837-1839 (2001)

Dimple Potential

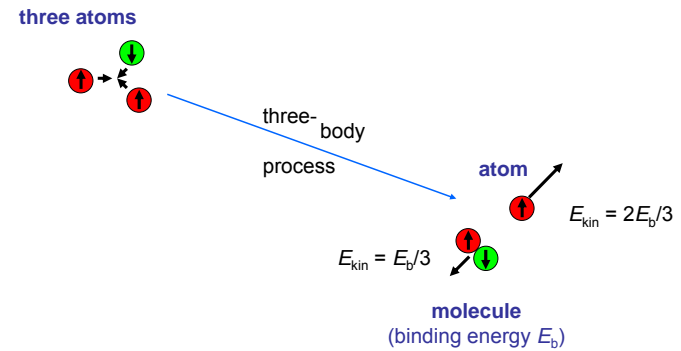


Evaporative cooling results



Three body recombination

...create molecules by collisions!

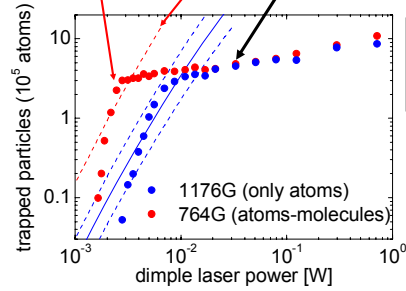


Evaporative cooling results

...now @ field where a weakly bound molecular state exists!

~ 2 molecules
per quantum state !!!

critical temperature
number of quantum states for molecules



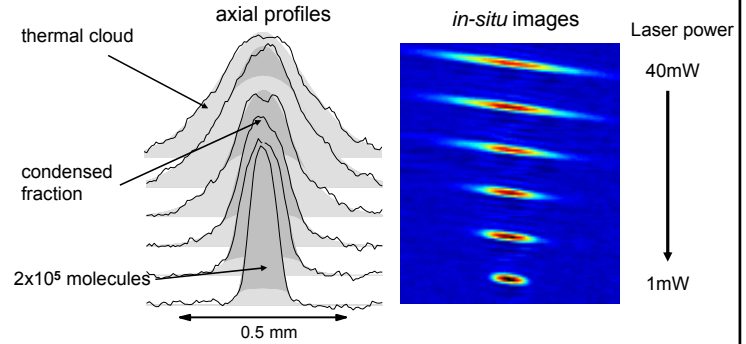
- quantum degeneracy !
- very long lifetime (~40s)
- thermalization

These molecules
must form a BEC!

S. Jochim *et al.*, Science **302**, 2101 (2003)

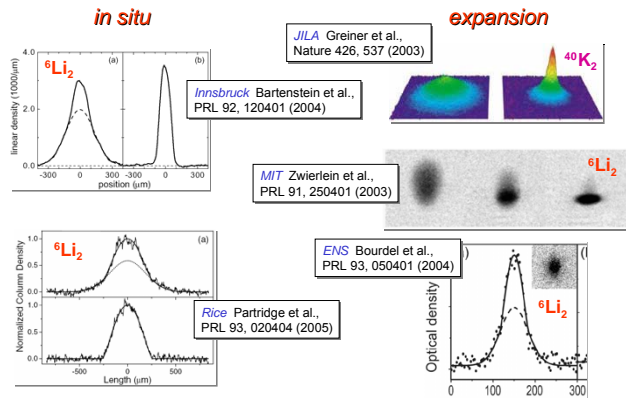
Bose-Einstein condensation

In-situ images of the molecules



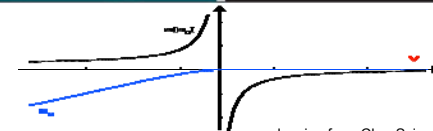
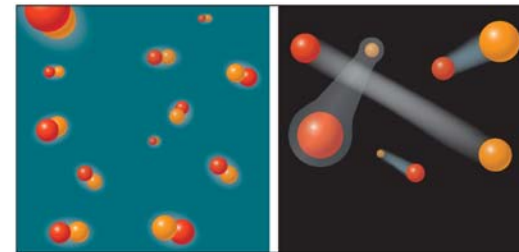
• molecular BEC was simultaneously achieved at JILA, Boulder

Molecular BEC gallery



BEC – BCS crossover

molecules **crossover** Cooper pairs
strong coupling weak coupling



drawing from Cho, Science **301**, 750 (2003)